Reproducible Research

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THE IMPORTANT THING IS TO STAY CALM AND TACKLE THE PROBLEMS ONE AT A TIME: FIRST, WE'LL CORRECT THE ERRORS IN OUR EQUATION, THEN WE'LL DEAL WITH THE WORMHOLE AND THE POODLES.

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The big bad wolf came to the first little scientist’s house and tried to blow it down. But the house was built of graphene, so was much too strong.

The second little scientist had built his house of ceramic meta-materials. Once again, the big bad wolf tried and failed to blow the house down.

The third little scientist had built his house of nano-engineered concrete. The big bad wolf blew and blew until he fell exhausted to the ground.

The scientists tagged the wolf, released him back into the wild and began a study of his habitat and behaviour.
Estimating the reproducibility of psychological science

Open Science Collaboration*†

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Open Science Collaboration study

• Replications of 100 experimental and correlational studies
• “The mean effect size (r) of the replication effects ($M_r = 0.197$, $SD = 0.257$) was half the magnitude of the mean effect size of the original effects ($M_r = 0.403$, $SD = 0.188$)”
• “97% of original studies had significant results ($P < .05$). 36% percent of replications had significant results”
• “47% of original effect sizes were in the 95% confidence interval of the replication effect size”
• “39% of effects were subjectively rated to have replicated the original result”
• “if no bias in original results is assumed, combining original and replication results left 68% with statistically significant effects”
Distribution of p-values

• P-value: the probability of observing an observation as extreme or more extreme than what was actually observed, assuming the null-hypothesis is true

• If the Null-Hypothesis is true, what is the probability that the p-value is smaller than 0.3?
Distribution of p-values

• P-value: the probability of observing an observation as extreme or more extreme than what was actually observed, assuming the null-hypothesis is true

• If the Null-Hypothesis is true, what is the probability that the p-value is smaller than 0.3?
  • 30% of the time, will get a value such that we’d get an even more extreme value 30% or less.
Distribution of p-value

- Some null-hypotheses are true, and some are false

If most of the hypotheses tested are actually false, most of the positive findings are false positives.
What percentage of hypotheses being test is false?

• Suppose the fraction of false null hypotheses is $\pi_0$
• Consider the distribution of the p-values for “positive” results ($p < 0.05$)
• The probability of seeing a particular p-value can be modelled as

\[ f(p|a, b, \pi_0) = \pi_0 \text{Unif}(0, 0.05) + (1 - \pi)t\text{Beta}(a, b; 0.05) \]

• $t\text{Beta}(a, b; 0.05)$ is the Beta distribution, truncated at 0.05
• Can now infer $\pi_0$ using a version of Maximum Likelihood
Intuition

• What kind of distribution of p-values would we expect if the null-hypothesis is true?

• What kind of distribution of p-values would we expect for the entire field, with some true hypotheses and some false hypotheses?
So what’s the false discovery rate?

- Original estimate: 15%
  - The model does not include bad faith or fraud
- Authors then acknowledged it may be higher